## MATH 221: Calculus and Analytic Geometry Prof. Ram, Fall 2004

## HOMEWORK 12: SELECTED ANSWERS

Problem A. Length of a plane curve.

(2)10.5 (3) 6a

(4) 12

 $(8/27)(10\sqrt{10}-1)$ (5)

(6) 14/3

 $(7) \quad 53/6$ 

(8) 123/32

(9)  $(4/27)(10\sqrt{10}-1)$ 

 $(10) \quad a\pi^2/8$ 

(11) 8

(12) 12

 $(13) \quad 21/2$ 

 $(14) \quad 27/20$ 

 $(15) \quad 19/3$ 

(16)  $f(x) = a \pm x\sqrt{A^2 - 1}, |A| > 1$ 

(17) No

Problem B. Surface area.

(2)  $4\pi^2 r^2$ 

 $(3) 99\pi/2$ 

(4)  $(\pi/27)(10\sqrt{10}-1)$ 

(5)  $(\pi/6)(17\sqrt{17}-1)$  (6)  $1823\pi/18$ 

 $(7) \quad 253\pi/20$ 

(8)  $(2\pi/3)(2\sqrt{2}-1)$  (9)  $12\pi a^2/5$  (10)  $(2\pi/3)(26\sqrt{26}-2\sqrt{2})$ 

(11)  $56\pi\sqrt{3}/5$  (12)  $424\pi/15$  (13)  $153\pi/40$ 

Problem C. Center of mass.

(1) At the intersection of the lines through each vertex which are perpendicular to the opposite side.

(2) At  $(0,(2/\pi)r,0)$  if the center is at (0,0) and the y-axis cuts the semicircle in half.

(3) At (0, (8/15)r, 0) if the hemisphere is sitting on the x-z plane with its apex at (0, r, 0).

1

(4)  $(4a/3\pi, 4a/3\pi)$  (5)  $(0, (2/5)h^2)$  (6)  $(2a/3(4-\pi), 2a/3(4-\pi))$ 

(7)	$(\pi/2, \pi/8)$	
(I)	(n/2, n/0)	

$$(8)$$
  $(2/5,1)$ 

(10)(3/5)h

- (11) On the axis of the cone 3h/4 from the vertex.
- (12) On the axis of the cone 3h/5 from the vertex.
- (13) At  $(0, \pi r/4)$  if the semicircle is positioned as in (2).
- (14) At (0, (3/8)r, 0) if the hemisphere is positioned as in (3).
- (15) At (0, (1/2)r, 0) if the hemisphere is positioned as in (3).

(16) 
$$(0, 2c^2/5)$$

$$(17) \quad (16/105, 8/15)$$

$$(18) \quad (0, 12/5)$$

$$(19) \quad (1, -3/5) \qquad (20) \quad (3/5, 1)$$

$$(20)$$
  $(3/5,1)$ 

(21) On the axis of the cone 3h/4 from the vertex.

$$(22) \quad (0,8/3)$$

$$(23)$$
  $(4/5,0)$ 

(24) On the axis of the cone 2h/3 from the vertex.

(25) 
$$(-r, 3r/(2+\pi))$$

$$(26) \quad (17\sqrt{17} - 1)/12$$

(27) 
$$(2r/\pi, 2r/\pi)$$

## Problem B. Average value of a function.

$$(2) \quad 50\frac{1}{2}$$

$$(3)$$
 126

$$(4)$$
 117

$$(5) \quad 21536939630755577663107.46$$

$$(10) \quad 2/\pi$$

$$(12)$$
  $\frac{1}{2}$ 

$$(13)$$
  $\frac{1}{2}$ 

$$(14)$$
  $49/12$ 

$$(15)$$
  $\frac{1}{2}$ 

$$(16) \quad \alpha \left(\frac{a+b}{2}\right) + \beta$$

$$(17a)$$
 200 cases

$$(18) \quad \frac{a}{3}(3\sqrt{3}-1)$$

(19a) 
$$\frac{2}{3}b^2$$

(19b) 
$$\frac{2}{3}b$$

$$(20b)$$
  $82\frac{2}{3}$ 

(21) 
$$50 + 28/\pi$$