

MATH 221: Calculus and Analytic Geometry
Prof. Ram, Fall 2006

HOMEWORK 5: SELECTED ANSWERS

Problem A. Evaluating limits when $x \rightarrow 0$.

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|----------------------|-------------------------------|-----------------------|------------------|
| (1) 10 | (2) 5 | (3) $17/2$ | (4) $-317/422$ |
| (5) $-3/5$ | (6) $\frac{1}{2\sqrt{x}}$ | (7) $1/2$ | (8) $\sqrt{2}/4$ |
| (9) $-(1/2)x^{-3/2}$ | (10) $2\sqrt{a}$ | (11) $1/2$ | (12) 2 |
| (13) 1 | (14) $\frac{a}{2\sqrt{ax+b}}$ | (15) $mn(mx+c)^{n-1}$ | |

Problem B. Evaluating limits when $x \rightarrow a$.

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|------------|----------------------------|---------------------|----------------------------|
| (1) 5 | (2) 14 | (3) -2 | (4) -11 |
| (5) 3 | (6) $1/2$ | (7) 4 | (8) 108 |
| (9) 3125 | (10) $12a^{11}$ | (11) $(5/2)a^{3/2}$ | (12) $(5/3)(a+2)^{2/3}$ |
| (13) 6 | (14) $20/3$ | (15) n | (16) $\frac{1}{2\sqrt{a}}$ |
| (17) $1/2$ | (18) $\frac{2\sqrt{3}}{9}$ | (19) na^{n-1} | |

Problem C. Evaluating limits as $x \rightarrow \infty$.

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|-----------|------------|-----------|-----------|--------|
| (1) 1 | (2) $3/5$ | (3) $1/3$ | (4) $2/7$ | (5) 12 |
| (6) $1/2$ | (7) $1/2$ | (8) 0 | (9) e | (10) 0 |
| (11) 0 | (12) $1/2$ | | | |

Problem D. Limits with exponential and log functions.

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|---------------------|-------------|-------|---------|
| (1) 1 | (2) $\ln a$ | (3) 1 | (4) e |
| (5) $\ln a - \ln b$ | (6) 1 | (7) 0 | |

(11) $\frac{1}{2\sqrt{x}} e^{\sqrt{x}}$ (12) $\frac{a}{ax+b}$ (13) $x^x(\ln x + 1)$

Problem E. Limits with trigonometric functions.

- (1) $3/4$ (2) $1/3$ (3) 1 (4) $1/2$ (5) a/b
(6) $1/4$ (7) m/n (8) 0 (9) $2/3$ (10) 1
(11) $1/2$ (12) $\cos a$ (13) 2 (14) $1/3$ (15) -2
(16) -2 (17) $1/6$ (18) 2 (20) $\cos a$ (21) 0

Problem G. Limits with inverse trigonometric functions.

- (1) $1/2$ (2) $-\sqrt{2}/2$ (3) $1/2$ (4) 0
(5) $2/3$